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\\ search in the text file list_fano_ge3.out for Q-Fanos X of Fano index  $q=qW(X)\ge 3$ 
\\ allocatemem(s=100000000);
infty=10^8;

FANO_INDEX_MIN=11;
FANO_INDEX_MAX=11;
("FANO_INDEX_MIN \\le qW(X) \\le FANO_INDEX_MAX ");

DIM_K_MIN=-1;
DIM_K_MAX=infty;
("DIM_K_MIN\\le dim |-K_X|\\le DIM_K_MAX");

DIM_A_MIN=-1;
DIM_A_MAX=infty;
("DIM_A_MIN\\le dim |A|\\le DIM_A_MAX");

DEGREE_MIN= 0;
DEGREE_MAX= 125/2;
("DEGREE_MIN\\le -K^3 \\le DEGREE_MAX");

LENGTH_OF_BASKET_MIN=0;
LENGTH_OF_BASKET_MAX=infty;
\\ LENGTH_OF_BASKET -- the length of the basket, should be \\le 15

KAWAMATA_BOGOMOLOV_BOUND_CHECK=0;
\\ check Kawamata-Bogomolov bound?
\\ if KAWAMATA_BOGOMOLOV_BOUND_CHECK=0, then Kawamata-Bogomolov bound will be not checked
\\ otherwise KAWAMATA_BOGOMOLOV_BOUND_CHECK= 1 , 2, 3
\\ put KAWAMATA_BOGOMOLOV_BOUND_CHECK=1 if  $qW(X)=qQ(X)$ 
\\ put KAWAMATA_BOGOMOLOV_BOUND_CHECK=2 if  $qW(X)\neq qQ(X)$ 
\\ put KAWAMATA_BOGOMOLOV_BOUND_CHECK=3 in general
INDEX_FANO_MAXXX=50;
INDEX_FANO_SET=Set({[3,4,5,6,7,8,9,10,11,13,17,19]});
N_INDEX_FANO_SET=matsize(INDEX_FANO_SET)[2];
INDEX_FANO_MAX=0;
for (i=1, N_INDEX_FANO_SET, INDEX_FANO_MAX=max(INDEX_FANO_MAX, eval(INDEX_FANO_SET[i])));
\\this is to check Kawamata-Bogomolov bound
\\ we use  $t\ge 1/qQ$ 
\\ where  $qW$  divides  $qQ$  and  $qQ$  in INDEX_FANO_SET

p=1;
SUM_MIN=-infty;
("(\sum indices divisible by p) \ge SUM_MIN");

{
TEST=1; \\ for correct data
print("-----");
print("search for Q-Fanos X satisfying the following conditions:");

if (TEST && FANO_INDEX_MIN<>FANO_INDEX_MAX && FANO_INDEX_MIN<>-infty && FANO_INDEX_MAX<> infty,
print1(FANO_INDEX_MIN); print1(" \\le index Fano \\le "); print(FANO_INDEX_MAX));
if (TEST && FANO_INDEX_MIN<>FANO_INDEX_MAX && FANO_INDEX_MIN<>-infty && FANO_INDEX_MAX== infty,
print1(FANO_INDEX_MIN); print(" \\le index Fano"));
if (TEST && FANO_INDEX_MIN<>FANO_INDEX_MAX && FANO_INDEX_MIN== -infty && FANO_INDEX_MAX<> infty,
print1("index Fano \\le "); print(FANO_INDEX_MAX));
if (TEST && FANO_INDEX_MIN<>FANO_INDEX_MAX && FANO_INDEX_MIN== -infty && FANO_INDEX_MAX== infty, );
if (TEST && FANO_INDEX_MIN==FANO_INDEX_MAX, print1("index Fano= "); print(FANO_INDEX_MAX));
if ( FANO_INDEX_MIN>FANO_INDEX_MAX, print("WRONG DATA FOR index Fano"); TEST=0);

if (TEST && DEGREE_MIN<> -infty && DEGREE_MAX<> infty, print1(DEGREE_MIN); print1(" \\le -K_X^3 \\le ");

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print(DEGREE_MAX)););
if (TEST && DEGREE_MIN== -infy && DEGREE_MAX<> infy, print1(" -K_X^3 \\le "); print(DEGREE_MAX)););
if (TEST && DEGREE_MIN<> -infy && DEGREE_MAX== infy, print1(DEGREE_MIN); print(" \\le -K_X^3 "); );
if (TEST && DEGREE_MIN== -infy && DEGREE_MAX== infy,);
if (DEGREE_MIN > DEGREE_MAX, print(" WRONG DATA FOR -K_X^3 !!!"); TEST=0;);

if (TEST && DIM_K_MIN<>-infy && DIM_K_MAX<> infy && DIM_K_MIN<> DIM_K_MAX, print1(DIM_K_MIN);
print1(" \\le dim |-K_X| \\le "); print(DIM_K_MAX)););
if (TEST && DIM_K_MIN<>-infy && DIM_K_MAX<> infy && DIM_K_MIN= DIM_K_MAX, print1("dim |-K_X| = ");
print(DIM_K_MAX)););
if (TEST && DIM_K_MIN== -infy && DIM_K_MAX<> infy && DIM_K_MAX<> -infy, print1(" dim |-K_X| \\le ");
print(DIM_K_MAX)););
if (TEST && DIM_K_MIN<>-infy && DIM_K_MAX== infy, print1(DIM_K_MIN); print(" \\le dim |-K_X|"); );
if (TEST && DIM_K_MIN== -infy && DIM_K_MAX== infy,);
if (TEST && DIM_K_MIN== -infy && DIM_K_MAX== -infy, print(" dim |-K_X| -infy"); );
if ( DIM_K_MIN> DIM_K_MAX, print(" WRONG DATA FOR dim |-K_X| !!!"); TEST=0;);

if (TEST && DIM_A_MIN<>-infy && DIM_A_MAX<> infy && DIM_A_MIN= DIM_A_MAX, print1("dim |A|= ");
print(DIM_A_MAX)););
if (TEST && DIM_A_MIN<>-infy && DIM_A_MAX<> infy && DIM_A_MIN<> DIM_A_MAX, print1(DIM_A_MIN); print1("
\\le dim |A| \\le "); print(DIM_A_MAX)););
if (TEST && DIM_A_MIN== -infy && DIM_A_MAX<> infy && DIM_A_MAX<> -infy , print1(" dim |A| \\le ");
print(DIM_A_MAX)););
if (TEST && DIM_A_MIN<>-infy && DIM_A_MAX== infy, print1(DIM_A_MIN); print(" \\le dim |A| ")););
if (TEST && DIM_A_MIN== -infy && DIM_A_MAX== infy, );
if (TEST && DIM_A_MIN== -infy && DIM_A_MAX== -infy, print(" dim |A| = -infy")););
if ( DIM_A_MIN> DIM_A_MAX, print(" WRONG DATA FOR dim |A| !!!"); TEST=0;);

if (TEST && LENGTH_OF_BASKET_MIN <>-infy && LENGTH_OF_BASKET_MAX <> infy,
print1(LENGTH_OF_BASKET_MIN); print1("\\le (length of the basket)\\le "); print(LENGTH_OF_BASKET_MAX);
);
if (TEST && LENGTH_OF_BASKET_MIN == -infy && LENGTH_OF_BASKET_MAX <> infy, print1(" (length of the
basket)\\le "); print(LENGTH_OF_BASKET_MAX); );
if (TEST && LENGTH_OF_BASKET_MIN <>-infy && LENGTH_OF_BASKET_MAX == infy,
print1(LENGTH_OF_BASKET_MIN); print("\\le (length of the basket)"); );
if (TEST && LENGTH_OF_BASKET_MIN == -infy && LENGTH_OF_BASKET_MAX == infy,);
if (LENGTH_OF_BASKET_MIN> LENGTH_OF_BASKET_MAX, print(" WRONG DATA FOR length of the basket!!!");
TEST=0;);

if (TEST && KAWAMATA_BOGOMOLOV_BOUND_CHECK==2, print("Kawamata-Bogomolov bound is checked")););
if (TEST && KAWAMATA_BOGOMOLOV_BOUND_CHECK==1, print("Kawamata-Bogomolov bound is checked assuming
qW=q0")););
if (TEST && KAWAMATA_BOGOMOLOV_BOUND_CHECK==0, print("Kawamata-Bogomolov bound is NOT checked")););
if (TEST && KAWAMATA_BOGOMOLOV_BOUND_CHECK==3, print("Kawamata-Bogomolov bound is checked assuming
...")););
if ((KAWAMATA_BOGOMOLOV_BOUND_CHECK>3 || KAWAMATA_BOGOMOLOV_BOUND_CHECK<0),
print("KAWAMATA_BOGOMOLOV_BOUND_CHECK sould be 0,1, 2, or 3"); TEST=0;);

if (SUM_MIN<> -infy, print1(SUM_MIN); print1(" \\le (\sum indices divisible by "); print1(p);
print(")")););
if (TEST,
schetchik=0;

NN=matsize(readvec("list_fano_ge3.out"))[2];
\\ allocatemem(s=90000000);
for(i=1,NN,

FANO=readvec("list_fano_ge3.out")[i];

BASKET=FANO[1];

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GGI=FANO[2];
q=FANO[3];
A3=FANO[4];
Ac=FANO[5];
dimtAc=FANO[6];
LENGTH=FANO[7];
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\\ [BASKET,GGI ,q, A3, Ac, dimtAc, LENGTH]
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INDEX=vector(LENGTH, i, BASKET[i][1]);
WEIGHT=vector(LENGTH, i, BASKET[i][2]);
\\ WEIGHT[i] is the number b in [Reid, YPG]
\\ i.e. the quotient has the form  $1/r(1,-1,b)$ , where  $r=INDEX[i]$ 
dim_A=dimtAc[1];
dim_K=dimtAc[q];
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Kc=q*Ac;
K3=q^3*A3;
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TEST1=1;
TEST1= TEST1 && (q<=FANO_INDEX_MAX);
TEST1= TEST1 && (q>=FANO_INDEX_MIN);
TEST1= TEST1 && (K3<=DEGREE_MAX);
TEST1= TEST1 && (K3>=DEGREE_MIN);
TEST1= TEST1 && (LENGTH_OF_BASKET_MIN<=LENGTH);
TEST1= TEST1 && (LENGTH_OF_BASKET_MAX>=LENGTH);
TEST1= TEST1 && (dim_A<= DIM_A_MAX);
TEST1= TEST1 && (dim_A>= DIM_A_MIN);
TEST1= TEST1 && (dim_K<= DIM_K_MAX);
TEST1= TEST1 && (dim_K>= DIM_K_MIN);
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if(TEST1,
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bool=1;
if (p<>1,
SUM_INDICES=0;
for(i=1,LENGTH, if((INDEX[i]%p)==0, SUM_INDICES=SUM_INDICES+INDEX[i]); ) );
bool= bool && SUM_INDICES>=SUM_MIN);
```

```
\\ check Kawamata-Bogomolov bound
if (KAWAMATA_BOGOMOLOV_BOUND_CHECK>0,
qQ=q;
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if (KAWAMATA_BOGOMOLOV_BOUND_CHECK==2,
for (i=1,INDEX_FANO_MAX, if((i%q)==0 && setsearch(INDEX_FANO_SET,i), qQ=max(i,qQ)); ) );
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```
if (KAWAMATA_BOGOMOLOV_BOUND_CHECK==3,
for (i=1,INDEX_FANO_MAX, if((i%q)==0 && i<=INDEX_FANO_MAX, qQ=max(i,qQ)); ) );
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bogomolov=0;
bogomolov=bogomolov || (K3<=3*Kc);
bogomolov=bogomolov || (((1/qQ)*(4-3/qQ)*K3<=4*Kc));
bogomolov=bogomolov || (((1-1/qQ)*(1+3/qQ)*K3<=4*Kc));
bogomolov=bogomolov || (((1/qQ)*(2-3/qQ)*K3<=Kc));
bool = (bool && bogomolov);
);
```

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if(boool,
print("-----");
schetchik=schetchik+1;
\\ print the result

printp1("Q-Fano No. "); print(schetchik);
\\ printp1("LENGTH="); print(LENGTH);
printp1("qW(X)="); print(q);
printp1("BASKET="); printp(BASKET);

\\ WEIGHT_A is the weight of the generator
\\ i.e.  $A \sim \sum \text{WEIGHT\_A}[i] K_X$  near  $P_i$  and  $0 \leq \text{WEIGHT\_A}[i] < r$ 
WEIGHT_A=vector(LENGTH,i, (-bezout(q,INDEX[i])[1])) %INDEX[i]);
\\ printp1("WEIGHT_A="); printp(WEIGHT_A);

print1("INDICES="); print(INDEX);
printp1("A^3="); print(A3);

\\ print dim |tA|
for (t=1,q,
printp1(" dim |"); print1(t); print1("A|="); print(dimtAc[t]);
);

);
);
);

print("-----");
print1(schetchik); print(" matching Q-Fanos found");
, print("WRONG DATA !!!!!!!!!!!!!!!"););
}

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